

chapter **6** Length – Area – Volume

**Section 6.1 Revision**

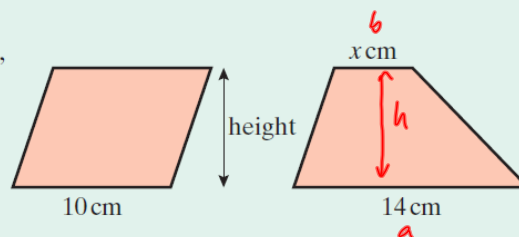
Area

$A = LB$   
 $\Delta = \frac{Bh}{2}$   
 $A = \pi r^2$   
 $V = LBH$   
 $V = \frac{\pi r^2 h}{3}$   
 $CSA = \pi r l$   
 $V = \pi r^2 h$   
 $CSA = 2\pi r h$   
 $V = \frac{4\pi r^3}{3}$   
 $SA = 4\pi r^2$

**1. Trapezium**

**Example 1**

If a parallelogram has a base of 10 cm, and a trapezium of the same area and height has a base of 14 cm, find  $x$ , the length of the other parallel side of the trapezium.



Trapezium

$$Area = \left(\frac{a+b}{2}\right)h$$

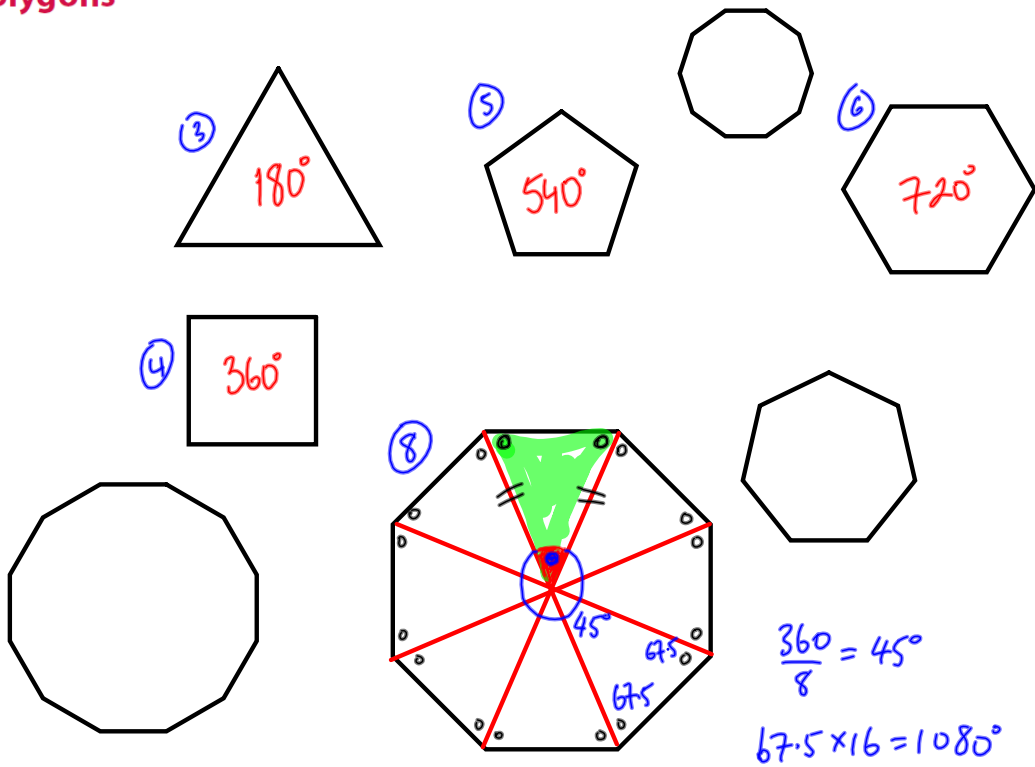
Area Parallelogram = Area Trapezium

$$10h = \frac{(x+14)h}{2}$$

$$20 = x + 14$$

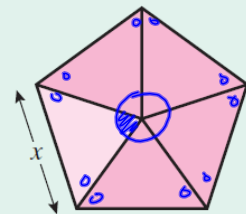
$$x = 6 \text{ cm}$$

2. Polygons

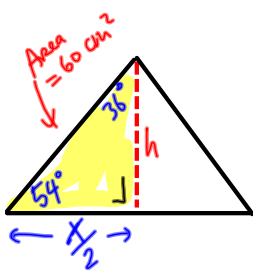


Example 2

The area of the regular pentagon shown here is  $600 \text{ cm}^2$ . Calculate the length of one side,  $x$ , of the pentagon.



Consider each triangle



$$\frac{360}{5} = 72^\circ$$

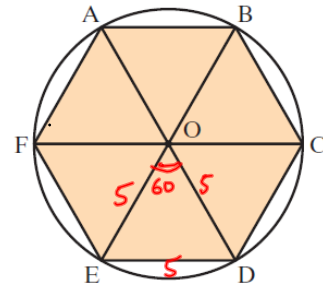
$$\text{Area} = \frac{600}{5} = 120 \text{ cm}^2$$

$$\tan 54 = \frac{h}{(x/2)} \Rightarrow h = \frac{x \tan 54}{2}$$

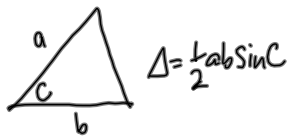
$$\Delta = \frac{Bh}{2} = \frac{(x/2)(x \tan 54)}{2} = 60$$

$$\Rightarrow x^2 \tan 54 = 480 \Rightarrow x = \sqrt{\frac{480}{\tan 54}} = 18.67$$

13. A regular hexagon is circumscribed by a circle of radius 5 cm. Find
- the size of the angle EOD
  - the size of the angle ODE
  - the area of the hexagon ABCDEFA.



720° in hexagon



$$(i) \angle EOD = \frac{360}{6} = 60^\circ$$

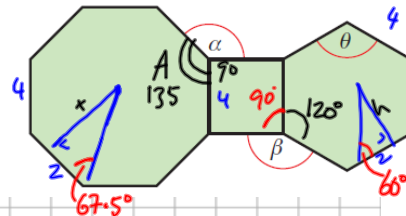
$$(ii) \angle OED = \frac{720}{12} = 60^\circ$$

$$(iii) \Delta = \frac{1}{2} (5)(5) \sin 60^\circ = 10.825$$

hexagon = 6 triangles

$$\Rightarrow \text{Area hexagon} = 10.825(6) = 64.951 \text{ cm}^2$$

14. A composite design of polygons is shown.
- Find the sizes of the angles  $\alpha$ ,  $\beta$ ,  $\theta$
  - If the square has a side of 4 cm, find the area of this composite shape correct to one place of decimals.



360° in square  
720° in hexagon  
1080° in octagon

TOA

$$\theta = \frac{720}{6} = 120^\circ$$

$$\beta = 360 - 90 - 120 = 150^\circ$$

$$A = \frac{1080}{8} = 135^\circ$$

$$\alpha = 360 - 135 - 90 = 135^\circ$$

octagon?

$$\Delta = \frac{Bh}{2}$$

6 Δs in octagon

$$\tan 67.5^\circ = \frac{x}{2} \Rightarrow x = 2 \tan 67.5 = 4.828$$

$$\Delta = \frac{2(4.828)}{2} = 4.828$$

$$\Rightarrow \text{Octagon Area} = 16(4.828) = 77.248$$

square?

$$A = L^2 = 4^2 = 16$$

hexagon?

$$\tan 60^\circ = \frac{h}{2} \Rightarrow h = 2 \tan 60^\circ = 2\sqrt{3}$$

$$\Delta = \frac{2(2\sqrt{3})}{2} = 2\sqrt{3}$$

$$\Rightarrow \text{Hexagon Area} = 12(2\sqrt{3}) = 24\sqrt{3}$$

12 Δs in hexagon

Total Area

$$= 77.248 + 16 + 24\sqrt{3} \approx 134.8 \text{ (1 dp)}$$